

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel
International GCSE**

Centre Number

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Candidate Number

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Thursday 18 June 2020

Morning (Time: 2 hours)

Paper Reference **4PM1/02R**

Further Pure Mathematics

Paper 2R



Calculators may be used.

Total Marks

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.
Anything you write on the formulae page will gain NO credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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Pearson

International GCSE in Further Pure Mathematics Formulae sheet

Mensuration

Surface area of sphere = $4\pi r^2$

Curved surface area of cone = $\pi r \times$ slant height

Volume of sphere = $\frac{4}{3}\pi r^3$

Series

Arithmetic series

Sum to n terms, $S_n = \frac{n}{2}[2a + (n - 1)d]$

Geometric series

Sum to n terms, $S_n = \frac{a(1 - r^n)}{(1 - r)}$

Sum to infinity, $S_\infty = \frac{a}{1 - r} \quad |r| < 1$

Binomial series

$$(1 + x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots \quad \text{for } |x| < 1, n \in \mathbb{Q}$$

Calculus

Quotient rule (differentiation)

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

Trigonometry

Cosine rule

In triangle ABC : $a^2 = b^2 + c^2 - 2bc \cos A$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A + B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A - B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A + B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A - B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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Question 2 continued

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(Total for Question 2 is 11 marks)



3

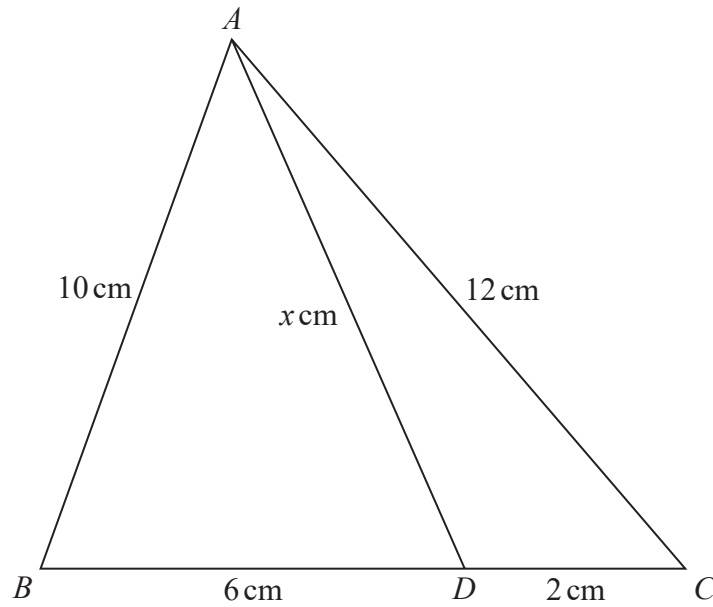


Diagram NOT accurately drawn

Figure 1

Figure 1 shows the triangle ABC in which $AB = 10$ cm and $AC = 12$ cm. The point D lies on BC such that $BD = 6$ cm, $DC = 2$ cm and $AD = x$ cm.

- (a) Show that $x = 11$ (4)

- (b) Find the area, in cm^2 to 3 significant figures, of triangle ADB . (4)

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Question 3 continued

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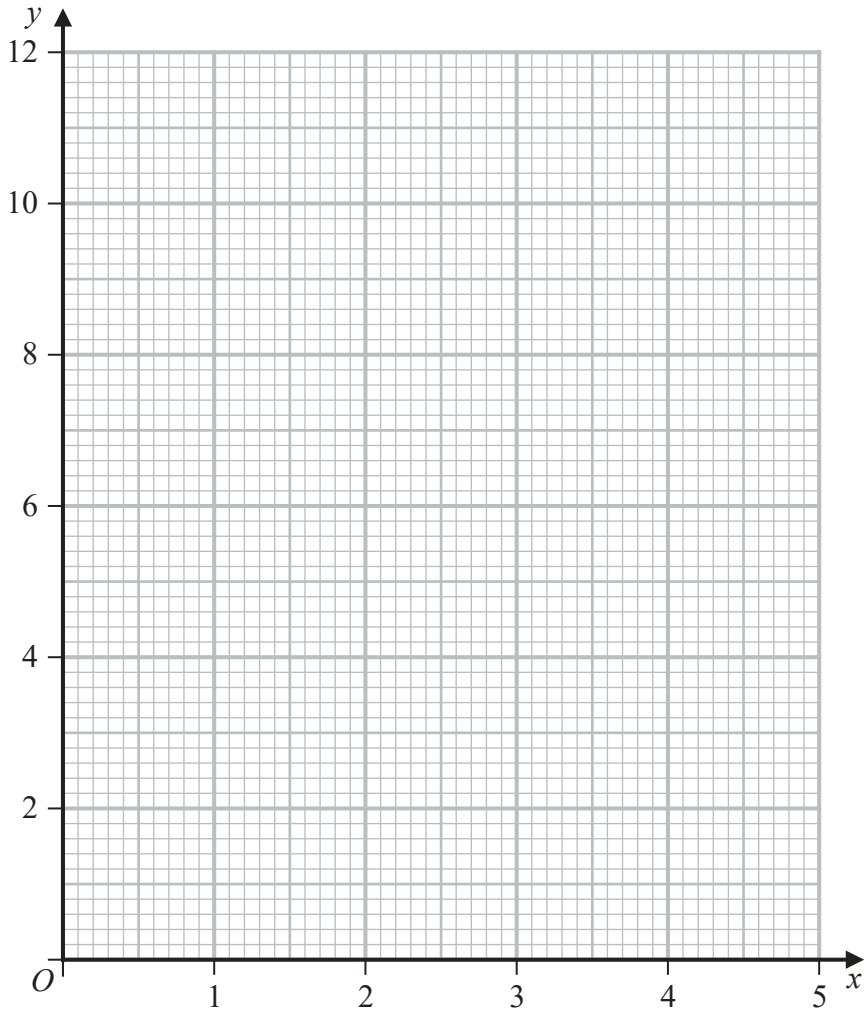
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(Total for Question 3 is 8 marks)



Question 4 continued



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Handwriting practice area consisting of 12 horizontal dotted lines.

Turn over for a spare grid if you need to redraw your graph.



Question 4 continued

Handwriting practice area consisting of 25 horizontal dotted lines.

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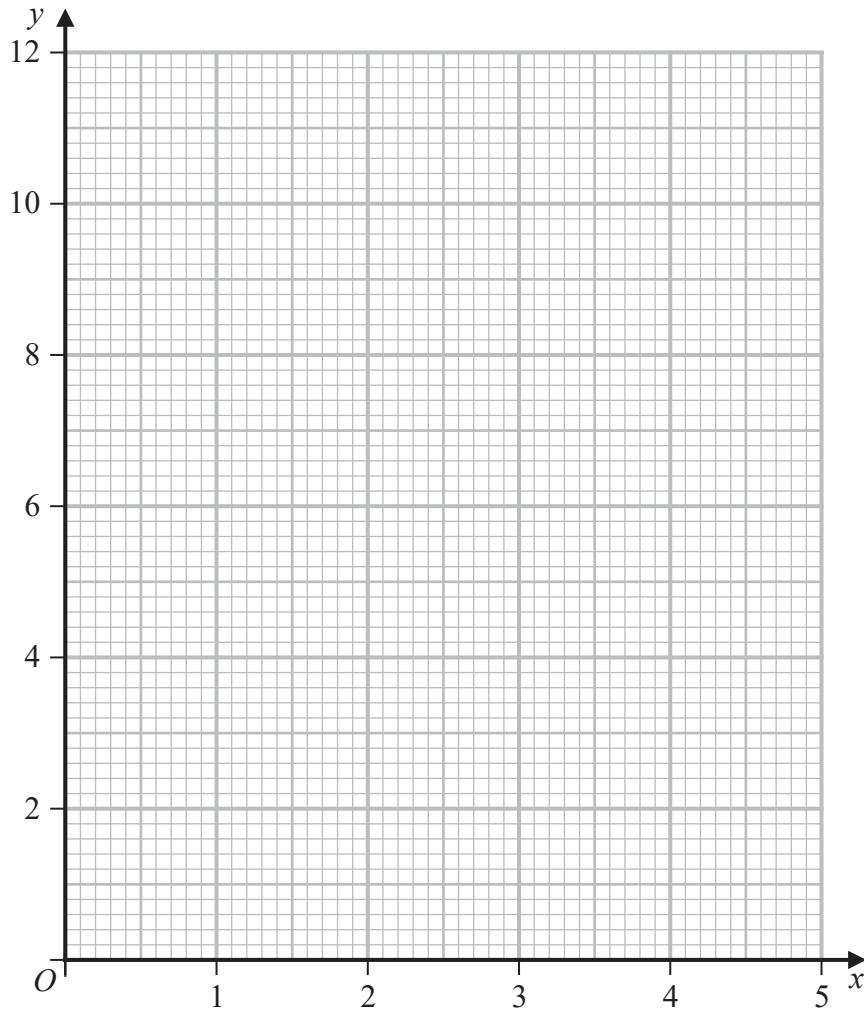
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Question 4 continued

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(Total for Question 4 is 11 marks)



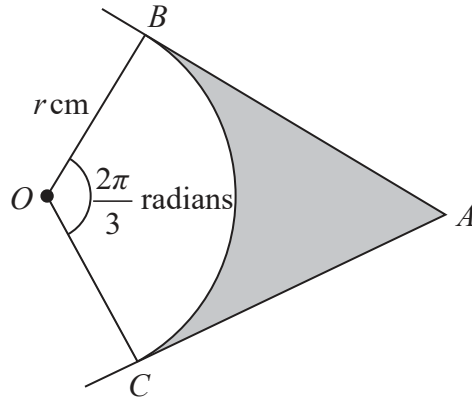


Diagram **NOT**
accurately drawn

Figure 2

In Figure 2, AB and AC are tangents to a circle with centre O and radius r cm.

The points B and C lie on the circle so that OBC is a sector of this circle and $\angle BOC = \frac{2\pi}{3}$ radians.

Given that the area of the shaded region is 10 cm^2 ,

find, to 3 significant figures, the value of r .

(8)

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Question 5 continued

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(Total for Question 5 is 8 marks)



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6

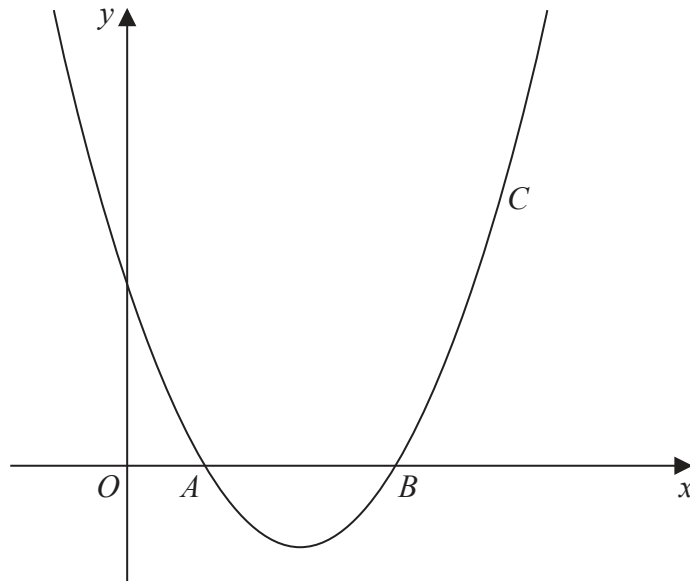


Diagram NOT accurately drawn

Figure 3

The curve C with equation $y = x^2 - 5x + 4$ crosses the x -axis at the points A and B , as shown in Figure 3

- (a) Find the coordinates of A and the coordinates of B . (3)

The tangent to C at A meets the tangent to C at B at the point T .

- (b) Find the coordinates of T . (6)

The normal to C at A meets the normal to C at B at the point N .

- (c) Find the coordinates of N . (3)

- (d) Find the area of the quadrilateral $ATBN$. (3)

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Question 6 continued

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Question 6 continued

Handwriting practice area consisting of 25 horizontal dotted lines.

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Question 6 continued

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(Total for Question 6 is 15 marks)



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Question 7 continued

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Question 7 continued

Area with horizontal dotted lines for writing.

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Question 7 continued

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(Total for Question 7 is 12 marks)



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Question 8 continued

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(Total for Question 8 is 7 marks)



9 Given that

$$x = e^{-t} \sin 2t$$

show that

$$\frac{d^2x}{dt^2} + 2\frac{dx}{dt} + 5x = 0 \quad (8)$$

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Question 9 continued

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Question 9 continued

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(Total for Question 9 is 8 marks)



$$f(x) = 32x^3 - 33x + 1$$

(a) Show that $f(1) = 0$ (1)

(b) Hence using an algebraic method solve $f(x) = 0$ (4)

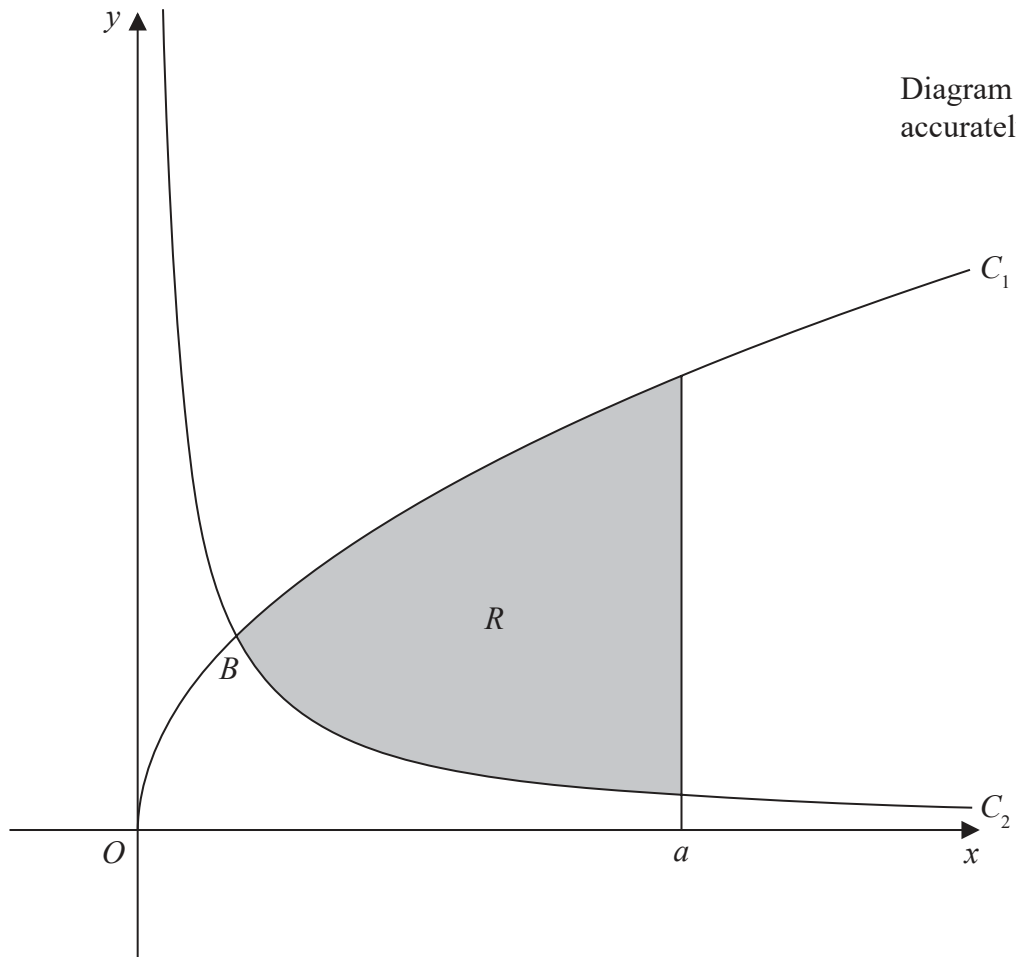


Figure 4

The region R , shown shaded in Figure 4, is bounded by the curve C_1 with equation $y = \sqrt{x}$, by the curve C_2 with equation $y = \frac{1}{8x}$ and by the line with equation $x = a$

The curves C_1 and C_2 intersect at the point B , with x coordinate p , where $p < a$

(c) Find the value of p . (2)

The region R is rotated through 360° about the x -axis to generate a solid with volume $\frac{27\pi}{64}$

(d) Use algebraic integration to find the value of a . (7)



Question 10 continued

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Question 10 continued

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Question 10 continued

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